

# Nonlinear Surface Magnetoplasmonics in Kretschmann Multilayers

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Supporting Information

**ABSTRACT:** Nonlinear magnetoplasmonics aims to utilize plasmonic excitations to control the mechanisms and tailor the efficiencies of nonlinear light frequency conversion at the nanoscale. We investigate the mechanisms of magnetic second-harmonic generation in hybrid gold–cobalt–silver multilayer structures, which support propagating surface plasmon polaritons at both fundamental and second-harmonic frequencies. Using magneto-optical spectroscopy in Kretschmann geometry, we show that the huge magneto-optical modulation of the second-harmonic intensity is dominated by the excitation of surface plasmon polaritons at the second-harmonic frequency, as shown by



tuning the optical wavelength over the spectral region of strong plasmonic dispersion. Our proof-of-principle experiment highlights bright prospects of nonlinear magnetoplasmonics and contributes to the general understanding of the nonlinear optics of magnetic surfaces and interfaces.

**KEYWORDS:** nonlinear optics, magnetoplasmonics, surface plasmon resonance, magnetophotonics, Kretschmann geometry, nanotechnology

Rapid development of plasmonics has facilitated an outstanding progress in understanding, designing, and controlling the optical response of metallic nanostructures, including that in the nonlinear-optical domain.<sup>1-4</sup> The optical second-harmonic generation (SHG) from solid interfaces represents a well-known experimental technique with numerous applications in physics, chemistry, and biology. Being a natural tool to enhance the light-matter interaction, the plasmon-assisted localization of the electric field in small volumes proved to be very effective at elevating the efficiency of nonlinear-optical processes. Beyond the physics of plasmonic nanoantennas requiring the fabrication of sophisticated metallic nanoobjects,<sup>5,6</sup> the Kretschmann geometry for the excitation of surface plasmon polaritons (SPPs) in a thin metallic layer on a dielectric prism plays a special role due to its robustness and simplicity.<sup>7</sup> A huge plasmonic enhancement of the electric field caused by the phase-matched excitation of SPPs under resonant coupling conditions has been shown to boost the SHG intensity.<sup>8–10</sup> The most recent experiments have evidenced that not only the SPP resonance at a fundamental frequency  $\omega$  but also the excitation of a second harmonic SPP at the doubled frequency  $2\omega$  play an important role in the process of nonlinear-optical conversion.<sup>10,11</sup>

Here we design a nanoscale optical experiment where we could excite, detect, and manipulate the nonlinear interactions between the SPPs at the fundamental and SHG frequencies. The main idea of this study was to demonstrate the rich, yet unexplored opportunities provided by the nonlinear magnetoplasmonics. While a few works report sizable modulation of the magnetic SHG output mediated by the SPP excitation at the fundamental frequency  $\omega$  only,<sup>13–16</sup> our experimental approach allows for the first time a direct comparison of the magnetic SHG effects driven by the SPPs excited at either  $\omega$  or  $2\omega$ . We demonstrate that the SPP excitation at the SHG frequency  $2\omega$  allows enhancing the magneto-optical modulation of the SHG output significantly, thus driving the magnetic contrast up to 33%.

In this work we have adopted the concepts of linear magnetoplasmonics in hybrid metal-ferromagnet multilayer structures<sup>3,12</sup> together with the most recent ideas in nonlinear plasmonics.<sup>10,11,15,17,18</sup> Our experimental geometry is sketched in Figure 1a. A thin gold/cobalt/silver trilayer structure was grown on a glass substrate by means of the magnetron sputtering. A 5 nm thin magneto-optically active layer of ferromagnetic cobalt was protected from oxidation by a 3 nm thin layer of gold. A 25 nm thick silver layer acted as the main constituent in this hybrid plasmonic nanostructure, which was excited by collimated femtosecond laser pulses through the glass prism (Kretschmann geometry). The reflected SHG intensity, as well as the linear reflectivity signal at both fundamental  $\omega$  and double frequency  $2\omega$ , was recorded as a function of the incidence angle  $\theta$  for the two opposite in-plane

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**Figure 1.** Surface plasmons in Au/Co/Ag multilayer structures. (a) Sketch of the experimental geometry showing the spatial distribution of the square of the normal projection of the electric field at the angles of incidence  $\theta$  corresponding to the SPP excitations at the fundamental  $\omega$  and double  $2\omega$  frequencies. Insets in the colored circles show the experimental angular dependencies of the linear-optical reflectivity and SHG intensities for the two opposite directions of magnetization of the cobalt layer. (b) Dispersion of the SPP in the Au/Co/Ag trilayer under study. Black dashed and green solid lines represent the photons in a vacuum and in glass, respectively. The thick dotted purple line is the calculated SPP dispersion; its line width is shown with the purple background area. The inset illustrates the possibility of a simultaneous excitation of the SPPs at both frequencies  $\omega$  and  $2\omega$ . The dispersion shown here is calculated within the effective media approximation developed in ref 1. The use of this approach is justified in the Supporting Information, where these calculations are compared with the results of the finite difference time domain calculations.



Figure 2. Angular spectra of the linear and nonlinear magneto-optical response in the presence of the SPPs. (a, b) Linear-optical reflectivity *R* and magnetization-induced reflectivity variations  $\Delta R/R$  for the excitation with the 920 and 460 nm wavelengths. (c, d) SHG intensity and (d) mSHG contrast  $\rho$  angular spectra plotted with an offset. Red and blue background areas illustrate the SPP dispersion in the experimental spectral range (760–920 nm for the fundamental, 380–460 for the SHG, respectively.) (e) Angular spectra of the mSHG magnetic contrast  $\rho$  for the four fundamental wavelengths; no offset is introduced.

directions of magnetization (+M and - M in Figure 1a) of cobalt in the transverse Kerr geometry.

Understanding the properties of the SPP dispersion<sup>19,20</sup> in our structure (see Figure 1b and Supporting Information for details) is one of the key points for nonlinear magnetoplasmonics. Due to inevitable dispersion, the SPP excitations at fundamental and double frequencies in Kretschmann geometry occur at slightly different angles, suggesting that simultaneous phase-matched excitation of both SPPs is impossible. However, nonlinear-optical considerations account for the following nonlinear phase-matching condition

$$2k_0(\omega) \ n(\omega) \sin \theta_{\rm nl} = k_{\rm spp}(2\omega) \tag{1}$$

between the excitation source at the silver–glass interface characterized by the in-plane component of the *k*-vector  $k_0^{\omega}$  sin  $\theta$  and the second-harmonic SPP at the gold–air interface with the *k*-vector  $k_{spp}^{2\omega}$ . Being just one of several possible SPP frequency conversion pathways,<sup>10,21</sup> this phase-matching condition plays a crucial role in our interpretation, as it determines the resonant SPP-induced enhancement of the nonlinear susceptibility  $\chi^{(2)}$ .

The experimental results are summarized in Figure 2. The linear optical reflectivities in Kretschmann configuration using the fundamental (920 nm) and second-harmonic wavelengths (460 nm, frequency doubled in a BBO crystal) are displayed in Figure 2a. A narrow plasmonic reflectivity dip at 920 nm observed at 42.5° contrasts with a much broader minimum at 460 nm at  $\theta \approx 47^{\circ}$ , in agreement with much higher SPP losses at 2 $\omega$ . In terms of linear magnetoplasmonics these two resonances behave similarly: the relative magnetization-induced variations of the reflectivity d $R/d\theta$ , suggesting that altering the magnetization direction induces a small shift of the reflectivity spectrum due to the magnetic contribution to the SPP wavevector.<sup>1,22</sup>

Whereas the linear reflectivity at fundamental frequency  $\omega$  shows only small modulations on the order of 1%, in line with ref 3, the SHG angular spectra at  $2\omega$  display drastic changes, as shown in Figure 2b for four different values of the fundamental wavelength 760, 800, 860, and 920 nm. Red and blue



**Figure 3.** Schematics of the SPP-assisted mSHG generation in a multilayer structure. (a) Illustration of the origin of the inequality of the SHG intensities for the opposite direction of the external magnetic field *H* leading to the nonzero magnetic contrast  $\rho$ . (b) SHG sources at the two interfaces, bottom (1, glass/Ag) and top (2, air/Au/Co/Si). (c, d) False-color spatial distributions of the square of the electric field projections  $|E_z|^2$  and  $|E_x|^2$  at the 860 nm fundamental wavelength. Dashed white lines show the sample borders. Solid white lines represent the corresponding  $|E|^2$  angular distributions at the top and bottom interfaces. (e, f) SHG intensity for the two opposite directions of the external magnetic field (red and blue symbols) and mSHG contrast angular spectra (green open circles) for the 860 nm fundamental wavelength together with the fit lines based on eq 3. Dashed lines are the angular profiles corresponding to the resonant SPP excitation at the frequency  $\omega$  and nonlinear SPP excitation  $\omega \rightarrow 2\omega$  (see Figure 5S in the Supporting Information).

background areas show the SPP dispersion (see Figure 1b) at the frequencies  $\omega$  and  $2\omega$ , respectively, recalculated as a function of incidence angle  $\theta$ . Over the SHG wavelengths range (380–460 nm) the SPP shows a strongly dispersive behavior, resulting in a shift of the resonant angle and decrease of losses (see the line width). The fundamental SPP remains nearly dispersionless and demonstrates no noticeable change of its line width. Contrary to previously reported results on a gold film,<sup>11</sup> the angular positions of the SPP resonances for the fundamental and SHG frequencies in our multilayer structure correspond to the pronounced minima in the SHG intensity. A strong dependence of SHG intensity on magnetization direction  $I_{2\omega}(\pm M)$  is quantified by the magnetic SHG (mSHG) contrast  $\rho$ :

$$\rho = \frac{I_{2\omega}(+M) - I_{2\omega}(-M)}{I_{2\omega}(+M) + I_{2\omega}(-M)}$$
(2)

shown in Figure 2d. Surprisingly, the largest magnetizationinduced modulation of the SHG intensity is accompanied by the SPP excitation at the SHG frequency and not the fundamental one. Angular dependence of mSHG contrast replotted in Figure 2e without an offset displays the largest reported values of modulation, reaching 33% around  $\theta = 44^{\circ}$ . For the shortest wavelength (760 nm) the mSHG maximum is only about 20%, since in this case the SPP damping at the SHG frequency becomes so large that the system approaches the region with the nonpropagating (propagation length  $\lambda^{\text{SPP}}$  <  $\lambda_{2\omega}$ ) SPPs. This observation links up our measurements to the most recent results by Zheng et al.,<sup>15</sup> who reported similar values of the mSHG contrast on a 10 nm thin iron film on glass, a structure not supporting SPPs at the SHG frequency. This fact, along with the dispersive shift of the mSHG maximum, reinforces our conclusion that the 33%, large mSHG contrast (which is equivalent to the increase of the SHG intensity by a factor of 2 upon magnetization reversal) is dominated by the SPP resonance at the SHG frequency.

In order to understand these experimental observations, we have used the approach proposed by Palomba and Novotny,<sup>11</sup> who explained the complex angular dependence of the SHG intensity from a thin gold film on glass by an interference of two contributions coming from the gold–air and gold–glass interfaces. In our case (Figure 3a) the silver–sapphire interface acts as a source of the nonmagnetic SHG  $\vec{E}_1^{2\omega}$ , and the upper part consisting of Au and Co layers is assumed to generate the electric field  $\vec{E}_2^{2\omega}$  containing both magnetic  $\chi^{(2m)}$  and nonmagnetic  $\chi^{(2)}$  contributions. Thus, the total SHG intensity  $I_{2\omega}$  is described by

$$\begin{split} I_{2\omega} \propto |\vec{E}_1^{\ 2\omega} + \vec{E}_2^{\ 2\omega} \pm \vec{E}_{2m}^{\ 2\omega}| \\ = |\chi_1^{(2)}: \vec{E}_1 \vec{E}_1 + \chi_2^{(2)}: \vec{E}_2 \vec{E}_2 \pm \chi_2^{(2m)}: \vec{E}_2 \vec{E}_2|^2 \end{split}$$
(3)

where complex tensor components  $\chi_1^{(2)}$  and  $\chi_2^{(2)} \pm \chi_2^{(2m)}$  represent the effective optical nonlinearities at both interfaces. The angular dependences of the electric fields  $\vec{E}_1$  and  $\vec{E}_2$  at the fundamental frequency  $\omega$ , which are driving the SHG process at both interfaces, are calculated by the finite difference time domain method for the 860 nm excitation wavelength (see Figure 3c,d).

We note that eq 3 represents an interference of the SHG electric fields from the top and the bottom interfaces, where the generation efficiency is largely determined by the angular dependence of the electric field  $E(\theta)$  at the fundamental frequency. Although the excitation of SPP at the double frequency  $2\omega$  does not affect the electric fields  $E^{(\alpha)}$ , it results in a resonant contribution to the nonlinear susceptibility  $\chi^{(2)}$ .

Also, the magnetization reversal  $M \rightarrow -M$  only slightly changes the spatial distribution of the electric field  $E^{(\omega)}(z)$  and cannot induce large magnetization-induced modulation of the SHG output (see Supporting Information for details). The latter can be explained as an interference phenomenon between the magnetic contribution  $\chi^{(2m)}$  from the upper (Au/Co) interface with the nonmagnetic  $\chi^{(2)}$  contributions from both interfaces (Figure 3a,b). On the basis of these calculations, the modulation of SHG intensity in the vicinity of fundamental SPP resonance can be explained by destructive interference of two contributions,  $\vec{E}_1^{2\omega}$  and  $\vec{E}_2^{2\omega}$ .<sup>11</sup> The SHG intensity minimum around the fundamental SPP resonance at  $\theta = 42.5^{\circ}$  can be associated with the strong increase of  $\vec{E}_2$  in Figure 3c,d at the upper interface. This requires us to assume that the nonlinearity of the upper interface is smaller than the lower one. This assumption is substantiated by the independent SHG measurements without the prism coupler performed from both sides of the sample. The SHG output measured from the Ag side was several times higher than that from the Au/Co side (see Figure S4 in the Supporting Information for details). The absence of the magnetic SHG signal when probing from the Ag side proved the lack of sensitivity to the opposite interface.

The same explanation holds for the SHG minimum around  $\theta$  = 45° albeit for a different reason. We note that the nonlinear susceptibility  $\chi^{(2)}$  is known to acquire an SPP-induced resonant contribution,  $\chi^{(2)} = \chi^{(1)}_{nr} + \chi^{(2)23,24}_{res}$  with

$$\chi_{\rm res}^{(2)}(\theta) \propto \frac{1}{\theta - \theta_{\rm nl} + i\Gamma}$$
 (4)

Owing to this resonant contribution, the SHG field enhanced at the top interface destructively interferes with the one generated at the bottom interfaces, which explains the experimentally observed SHG intensity minimum. In order to understand the angular spectrum of this resonant contribution, we approximated it with the Lorentzian resonance line. The width  $\Gamma$  and the angular position  $\theta_{nl}$  of this resonance line was chosen according to the calculations shown in Figure 1b for the nonlinear SPP excitation at frequency  $2\omega$ , or 430 nm wavelength. This resonant shape successfully accounts for the large mSHG modulation at the angles corresponding to the nonlinear SPP excitation quantified by eq 1. On the basis of eq 3 we were able to fit the experimental angular spectra using the resonant part of the nonlinear susceptibility  $\chi_{res}^{(2)}$  only.

Leaving out the details of our fitting of eq 3 for the Supporting Information, where the choice of predominant  $\chi^{(2)}$ components (from the six nonzero ones, three magnetic and three nonmagnetic, at each interface) is also justified, we would like to claim to have obtained a good quantitative agreement between the theory and experiment both for angular dependence of the SHG intensity (Figure 3e) and for mSHG contrast (Figure 3f). Note that the mismatch between the experimental data and the fit curves occurs largely around the fundamental SPP resonance, where the resonant  $\chi^{(2)}$  contribution used in our simulations is hardly playing any role. A more sophisticated analysis involving a large number of fit parameters<sup>25</sup> could potentially yield better agreement with the experimental data at the angles about 42.5°, where the SPP at  $\omega$  is excited. Also, in the future it would be interesting to test the validity of our effective interface approach and thus estimate the error introduced hereby. However, such procedures are beyond the scope of this paper, which is largely focused on the large magneto-optical modulation offered by the SPP coupling at the SHG frequency.

On the basis of our numerical calculations, we can conclude that the large value (33%) of the mSHG contrast is dominated by the properties of SPP resonance at the SHG frequency. Thus, upon reversing the external magnetic field, the SHG output can be doubled, which opens up a new strategy for the design of nonlinear magnetophotonic devices operating at the nanoscale. The frequency dependence over the dispersive SPP spectral range clearly demonstrated that the maximum value of 33% mSHG contrast remains large, whereas its angular width decreases as the SHG resonance gets narrower and shifts toward the fundamental resonance.

In the given spectral range one would expect to reach further enhancement of mSHG contrast by systematically varying the individual thicknesses in this trilayer structure. The future route for investigations will imply moving toward the experiments in the telecom frequency range, which apart from the obvious technological importance would allow extending the magnetooptical investigations including the magnetization-induced third-harmonic generation. Moreover, expanding into the far-IR or THz spectral range, where the SPP dispersion is lower, would allow exploring the phase-matched magnetoplasmonic coupling between the SPPs at the fundamental and second-, third-, and higher-order harmonic frequencies. With the largest reported plasmon-assisted value of mSHG contrast of 33% we get closer to the dream of nonlinear magnetophotonic devices based on novel physical principles.

# ASSOCIATED CONTENT

## Supporting Information

The Supporting Information is available free of charge on the ACS Publications website at DOI: 10.1021/acsphotonics.5b00504.

Surface plasmon dispersion in Au/Co/Ag trilayers; linear reflectivity in the presence of SPP; nonlinear-optical SPP excitation; fitting experimental data (PDF)

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### Notes

The authors declare no competing financial interest.

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